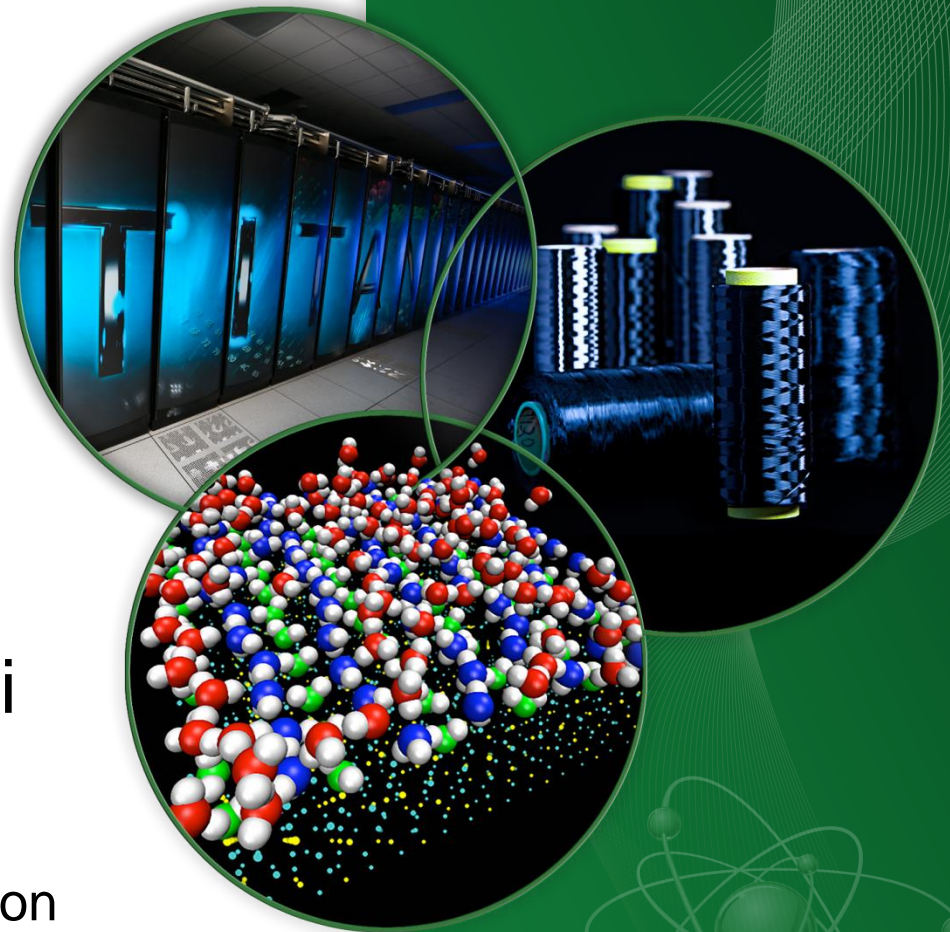


Development and Testing of Advanced S/U Methods for NCS Analyses

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Introduction

- Sensitivity coefficients describe the change in a system response that occurs due to uncertainty or perturbations in system parameters.

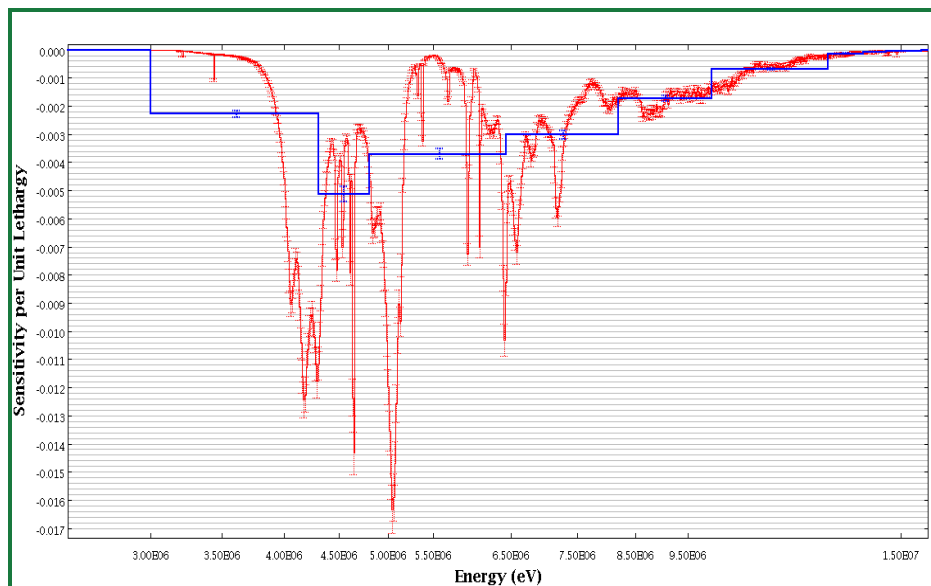
$$S_{R,\Sigma_x} = \frac{\delta R / R}{\delta \Sigma_x / \Sigma_x}$$

- The SCALE code contains a suite of eigenvalue (k_{eff}) sensitivity and uncertainty analysis tools using the TSUNAMI code, which has proven indispensable for numerous application and design studies for nuclear criticality safety and reactor physics.

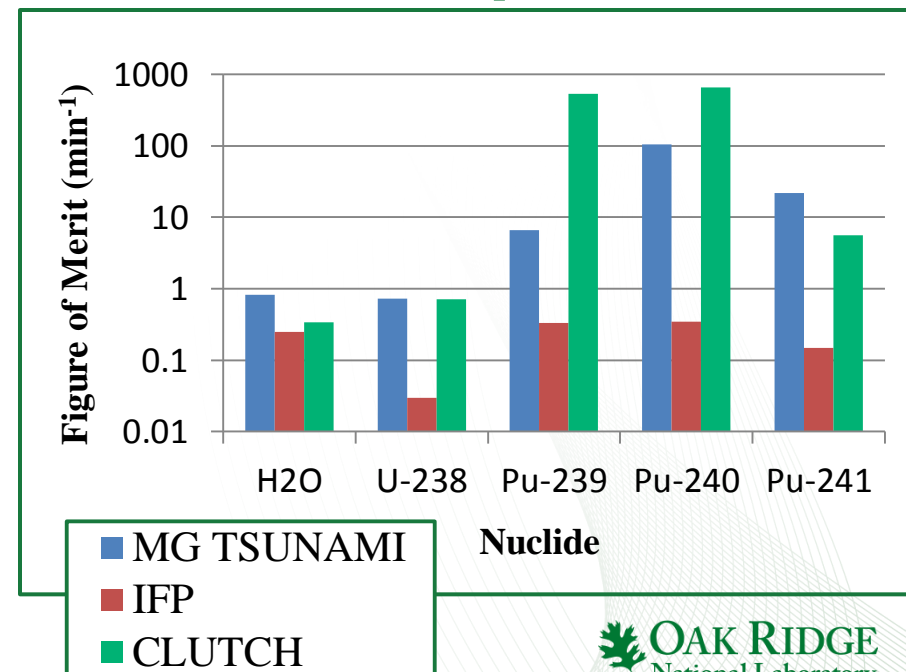
Introduction: Previous Work

- Recent NCSP-supported work has enabled the traditionally multigroup TSUNAMI-3D code to be extended to continuous-energy applications.
 - This work involved the development of the CLUTCH sensitivity method, a new and efficient approach for calculating eigenvalue sensitivity coefficients.

O-16 Capture Sensitivity 238-group VS Microgroup CLUTCH



MIX-COMP-THERM-004-001 FoM Comparison



Introduction

- This work has extended the Continuous-Energy (CE) TSUNAMI-3D eigenvalue sensitivity coefficient capabilities to enable a first-ever approach for calculating sensitivity coefficients for generalized neutronic responses in 3D, CE Monte Carlo simulations.
 - This was accomplished by combining the two approaches in CE TSUNAMI-3D for calculating eigenvalue sensitivity coefficients: the CLUTCH and Iterated Fission Probability (IFP) methods.
- This new generalized response sensitivity capability has been named the GEneralized Adjoint Responses in Monte Carlo (GEAR-MC) Method.

Generalized Perturbation Theory

- Generalized Perturbation Theory (GPT) estimates sensitivity coefficients for any system response that can be expressed as the ratio of reaction rates.

$$R = \frac{\langle \Sigma_1 \phi \rangle}{\langle \Sigma_2 \phi \rangle}$$

- Calculating generalized sensitivity coefficients requires solving an inhomogeneous, or generalized, adjoint equation:

$$L^\dagger \Gamma^\dagger = \lambda P^\dagger \Gamma^\dagger + S^\dagger$$

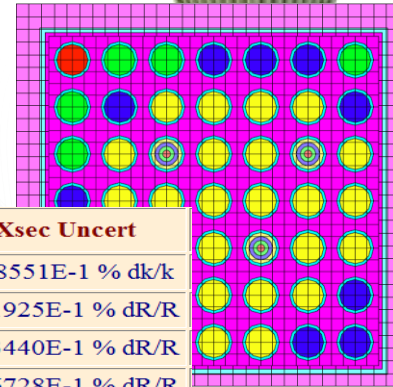
$$S^\dagger = \frac{1}{R} \frac{\partial R}{\partial \phi} = \frac{\Sigma_1}{\langle \Sigma_1 \phi \rangle} - \frac{\Sigma_2}{\langle \Sigma_2 \phi \rangle}$$

- Applications for GPT sensitivity/uncertainty analysis include:

- Relative Powers
- Isotope Conversion Ratios
- Multigroup Cross Sections
- Experimental Parameters

NUMBER	EXPERIMENT	Type	Format	Value	Xsec Uncert
1	k_infinity	keff	Relative	1.1083E+0	4.98551E-1 % dk/k
2	fission_grp_1	gpt	Relative	1.9155E-3	6.91925E-1 % dR/R
3	fission_grp_2	gpt	Relative	2.7748E-2	3.23440E-1 % dR/R
4	absorpt_grp_1	gpt	Relative	7.1637E-3	8.36728E-1 % dR/R
5	absorpt_grp_2	gpt	Relative	5.3702E-2	2.38082E-1 % dR/R
6	cornerrod_fpf	gpt	Relative	1.1458E+0	1.67147E-1 % dR/R

OECD UAM GPT Benchmark Phase 1-2 Results 



Theory

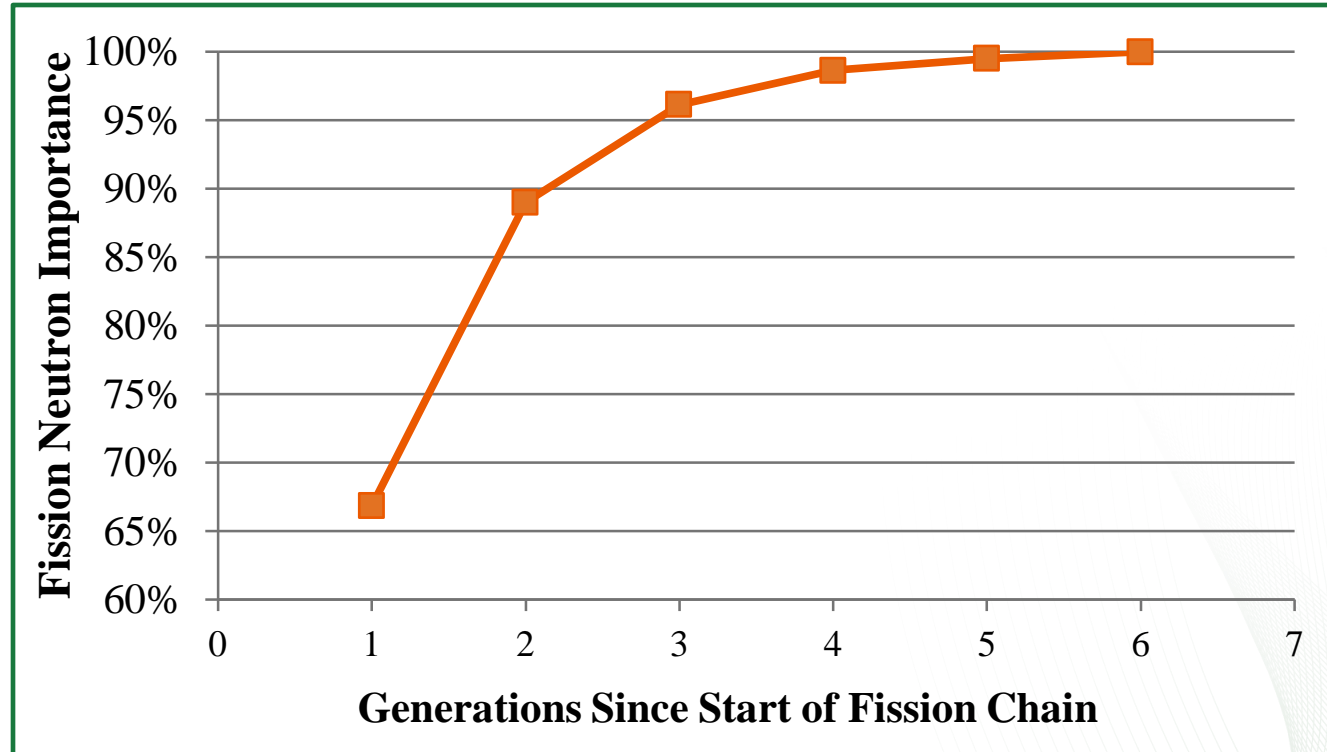
- The generalized importance function for a response can be expressed as the sum of two terms: the intra-generation effect term and the inter-generational effect term.
 - The **intra-generation** effect describes how much importance a neutron generates after an event occurs.
 - The **inter-generational** effect describes the importance that is generated by the daughter fission neutrons of the original particle.

$$\Gamma^{\dagger}(\tau_s) = \frac{1}{Q_s} \left\langle \frac{1}{R} \frac{\partial R}{\partial \phi}(r) \phi(\tau_s \rightarrow r) \right\rangle + \frac{\lambda}{Q_s} \left\langle \Gamma^{\dagger}(r) P(r) \phi(\tau_s \rightarrow r) \right\rangle$$

- The **CLUTCH** sensitivity method is used to calculate the intra-generation term, and an **Iterated Fission Probability**-based approach calculates the inter-generational term.
- $\frac{1}{R} \frac{\partial R}{\partial \phi}(r)$ contains both positive and negative terms. Thus, events during a particle history can generate either positive or negative importance.

Inter-generational Importance

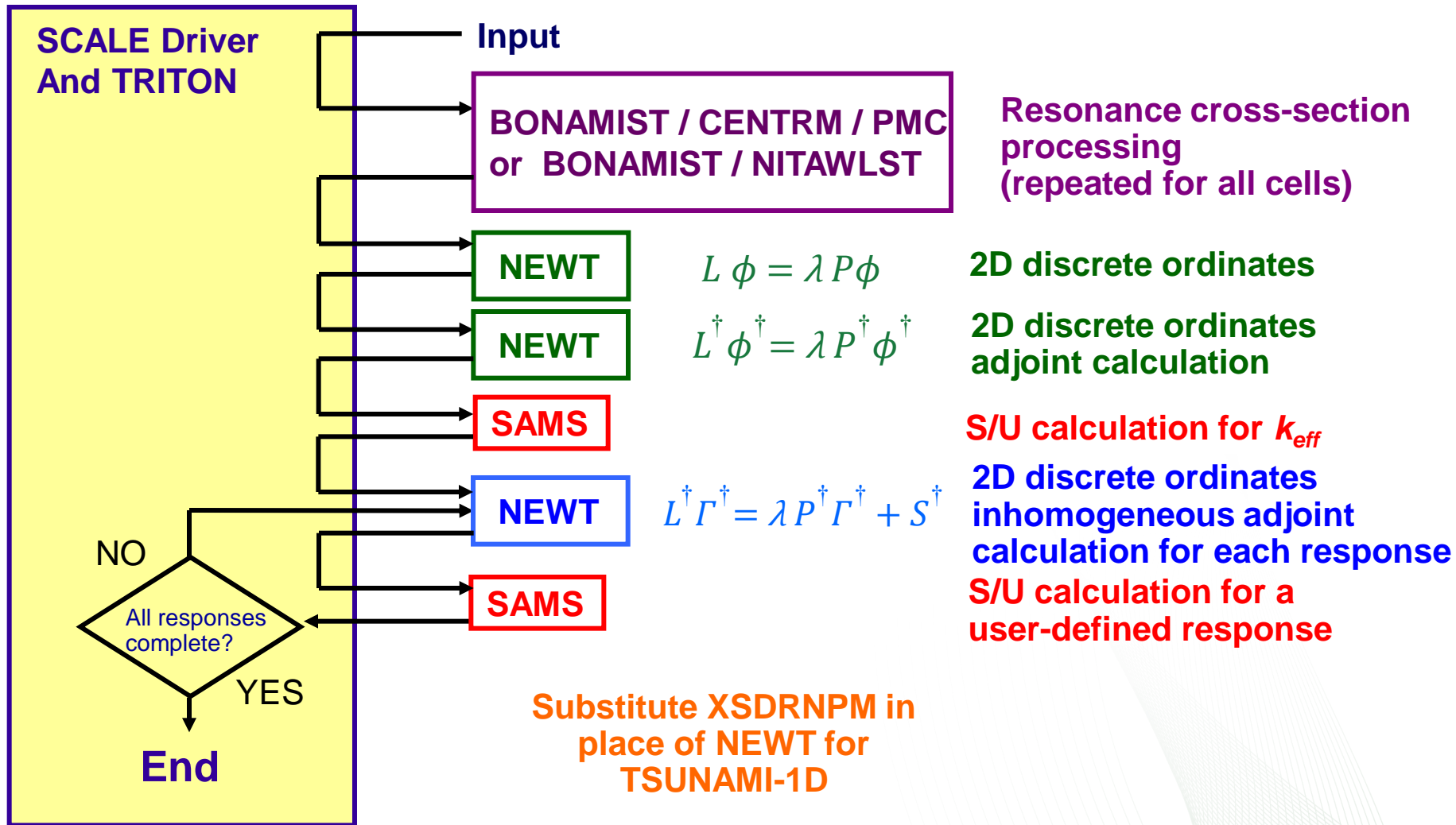
- The **inter-generational** term is calculated by tallying the intra-generational importance generated by neutrons in a fission chain as that importance approaches zero.
 - This term is tallied using the IFP method.



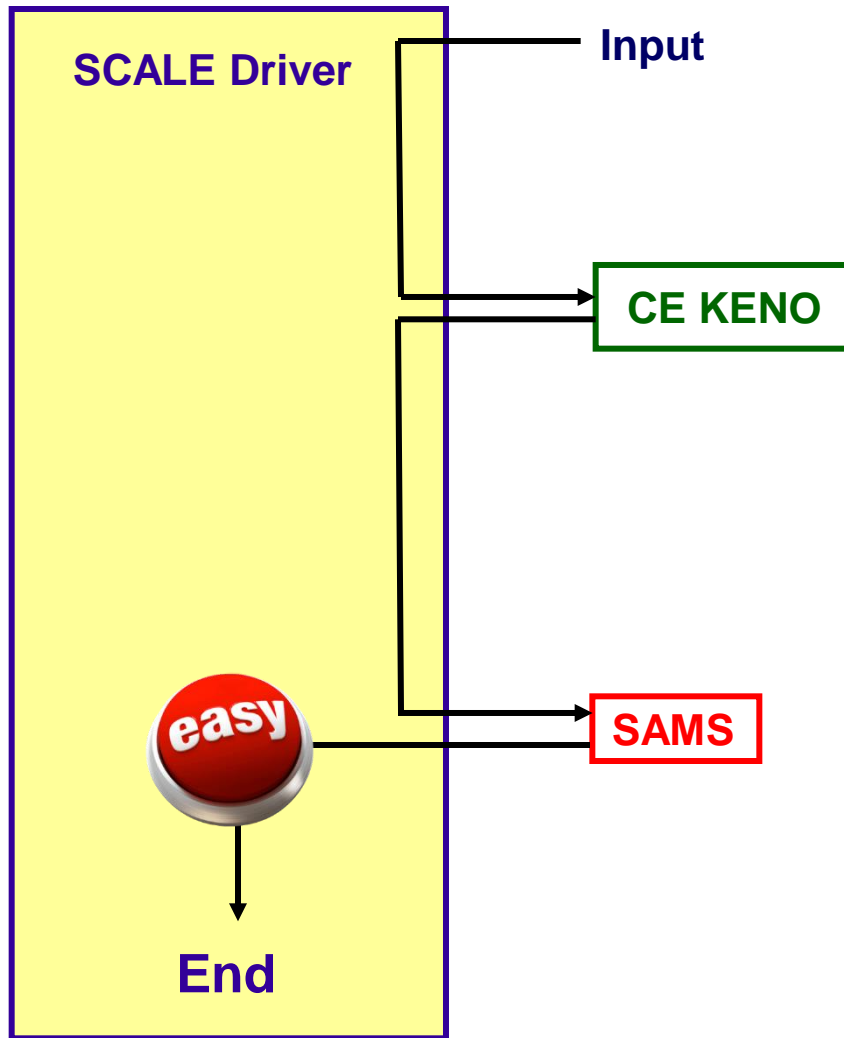
How does this approach differ from existing methods?

- Generalized Perturbation Theory Monte Carlo methods have been developed by Abdel-Khalik et al. for calculating generalized sensitivity coefficients in 3D, continuous-energy Monte Carlo applications, but these methods require performing multiple direct perturbation calculations and can require a large number of runs to calculate generalized sensitivity coefficients.
- This approach differs in that it:
 - Requires no perturbation calculations and no knowledge of nuclear covariance data.
 - Because our approach is not perturbation-based, we can easily calculate energy-dependent sensitivity coefficients for multiple responses to all input nuclear data parameters in one continuous-energy Monte Carlo transport calculation.
 - The deterministic, sensitivity-based TSUNAMI-1D and TSUNAMI-2D GPT methods require at least one transport calculation per generalized response.

TSUNAMI-1D/2D GPT Sequences



CE TSUNAMI-3D GPT Sequence



3D Monte Carlo

$$L \phi = \lambda P \phi$$

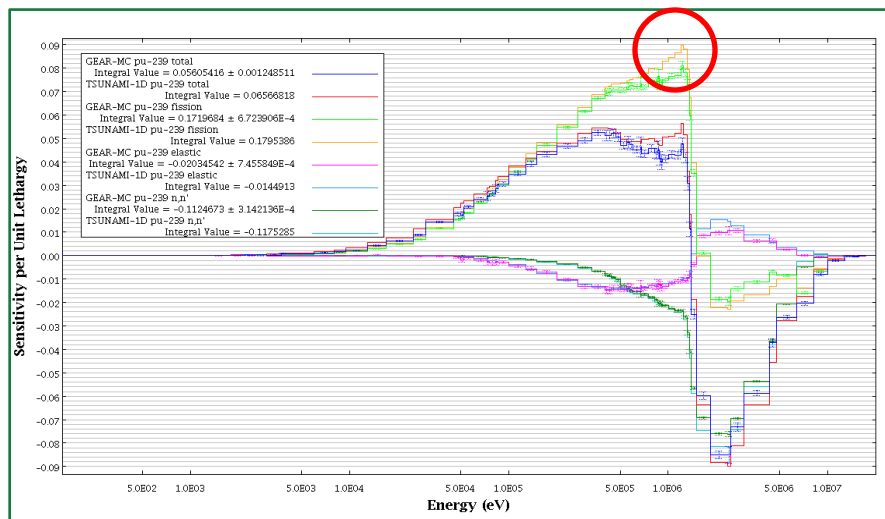
$$L^{\dagger} \phi^{\dagger} = \lambda P^{\dagger} \phi^{\dagger}$$

$$L^{\dagger} \Gamma^{\dagger} = \lambda P^{\dagger} \Gamma^{\dagger} + S^{\dagger}$$

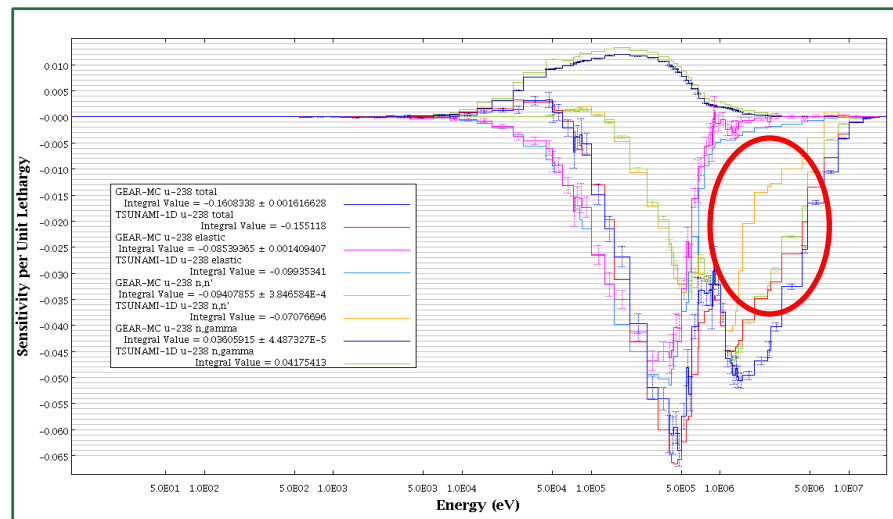
S/U calculation for k_{eff}
and user-defined
responses

GPT Flattop Foil Response Sensitivity Coefficients

F28/F25 Pu-239 Sensitivity Coefficients



F37/F25 U-238 Sensitivity Coefficients



Flattop Total Nuclide Foil Response Sensitivities

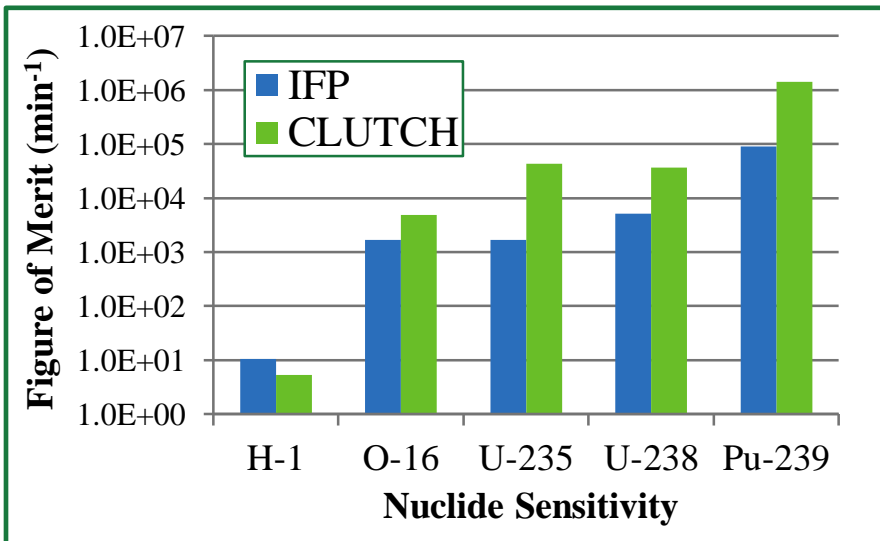
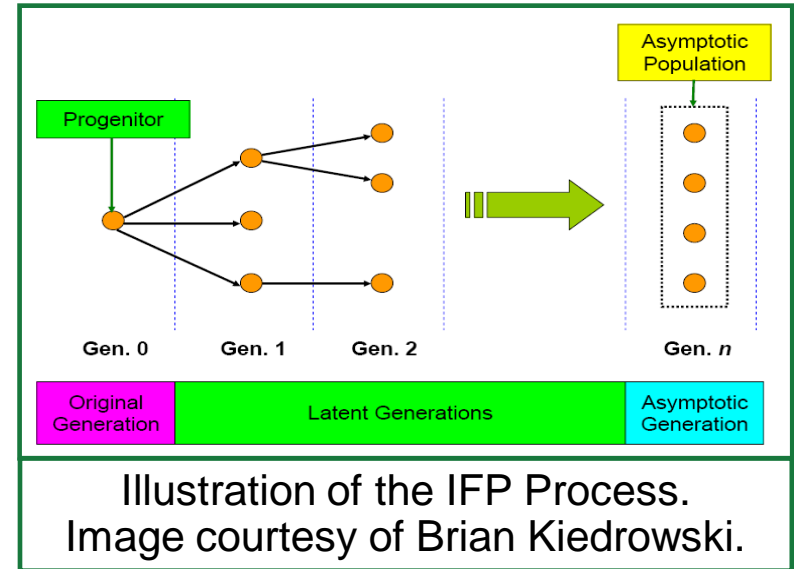
Experiment	Response	Isotope	Direct Pert.	TSUNAMI-1D	GEAR-MC
Flattop	F28 / F25	U-238	0.8006 ± 0.0533	0.8024 (0.03 σ)	0.7954 ± 0.0018 (-0.10 σ)
		Pu-239	0.0528 ± 0.0043	0.0657 (2.99 σ)	0.0561 ± 0.0012 (0.73 σ)
	F37 / F25	U-238	-0.1540 ± 0.0102	-0.1551 (-0.11 σ)	-0.1608 ± 0.0016 (-0.66 σ)
		Pu-239	0.0543 ± 0.0048	0.0736 (3.99 σ)	0.0489 ± 0.0010 (-1.10 σ)

Part Two:

GEAR-MC Efficiency Improvements

The IFP Method

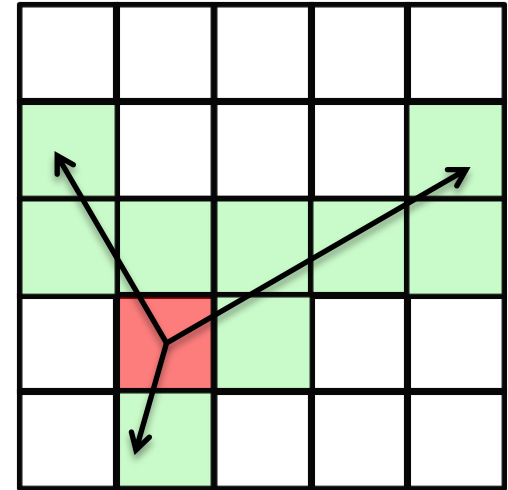
- Originally a modified version of the Iterated Fission Probability (IFP) Method was used to tally the **inter-generational** term.
- The IFP Method can produce large memory footprints for systems with a large number of materials, isotopes, etc.



Sensitivity Method Memory Usage		
Model	CLUTCH	IFP
Fuel Pin	1.06 MB	2,113 MB
Godiva	0.12 MB	26 MB
HMF-025-005	0.16 MB	1,675 MB
LCT-010-014	25 MB	19,509 MB
NAC-UMS	3,416 MB	21,201 MB

The $F^*(r)$ Function

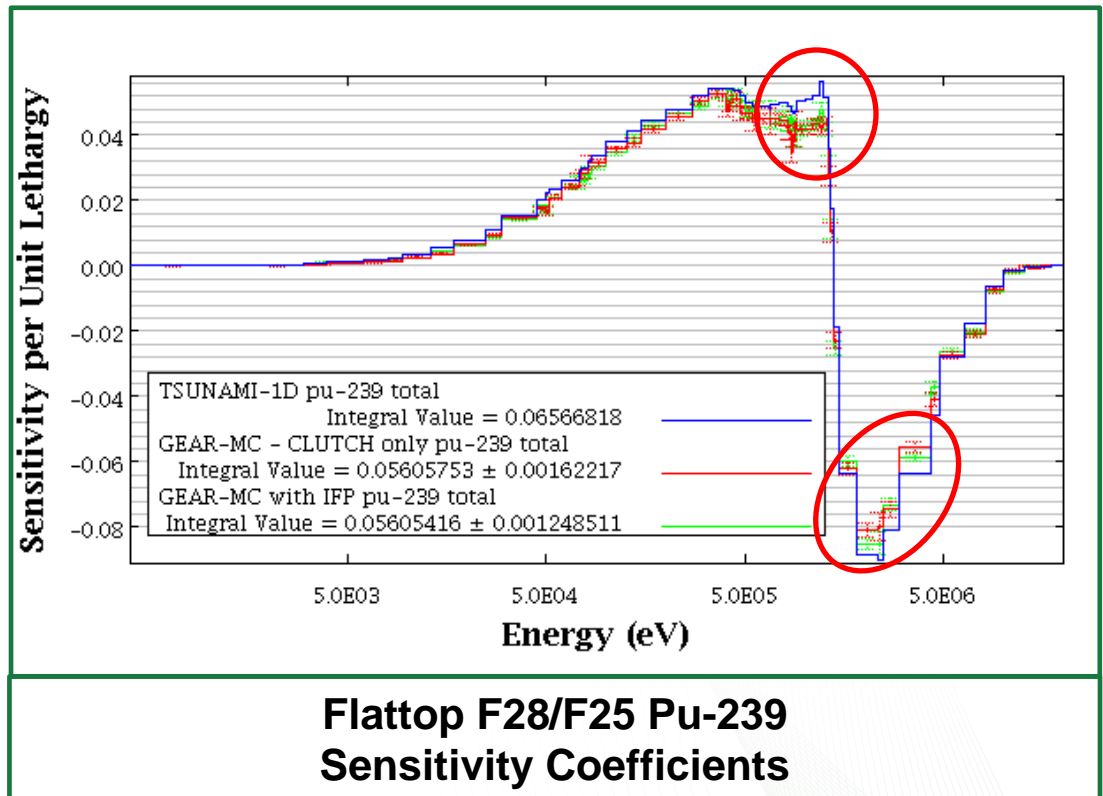
- The CLUTCH Method uses an importance weighting function, $F^*(r)$, to compute multi-generational sensitivity effects.
- The $F^*(r)$ function describes the average response importance generated by fission neutrons born at location r .
- The $F^*(r)$ function can be calculated using the IFP method during inactive generations with NO loss of accuracy and with significant memory savings.
- This work also sought to extend the concept of $F^*(r)$ to compute the inter-generational effect term in GEAR-MC GPT sensitivity calculations.



Evaluation of Accuracy: GPT Flattop Foil Response Sensitivity Coefficients

Generalized sensitivity coefficients were calculated for models of several criticality safety systems to:

- Evaluate the accuracy of the $F^*(r)$ approach.
- Explore the potential improvements in computational efficiency.



Evaluation of Accuracy: GPT Flattop Foil Response Sensitivity Coefficients

- The CLUTCH-only GEAR-MC calculations showed good agreement with both the conventional GEAR-MC and the reference Direct Perturbation sensitivity coefficients.

Experiment	Response	Isotope	Direct Pert.	TSU-1D	GEAR-MC with IFP	GEAR-MC CLUTCH only
Flattop	F28 / F25	U-238	0.8006 ± 0.0533	0.8024 (0.03 σ)	0.7954 ± 0.0018 (-0.10 σ)	0.7870 ± 0.0040 (-0.26 σ)
		Pu-239	0.0528 ± 0.0043	0.0657 (2.99 σ)	0.0561 ± 0.0012 (0.73 σ)	0.0561 ± 0.0016 (0.71 σ)
	F37 / F25	U-238	-0.1540 ± 0.0102	-0.1551 (-0.11 σ)	-0.1608 ± 0.0016 (-0.66 σ)	-0.1634 ± 0.0040 (-0.86 σ)
		Pu-239	0.0543 ± 0.0048	0.0736 (3.99 σ)	0.0489 ± 0.0010 (-1.10 σ)	0.0557 ± 0.0015 (0.27 σ)

Memory Usage

- Moving away from an IFP-based approach resulted in significant reductions in the computational memory footprint of simulations.

GEAR-MC Memory Usage

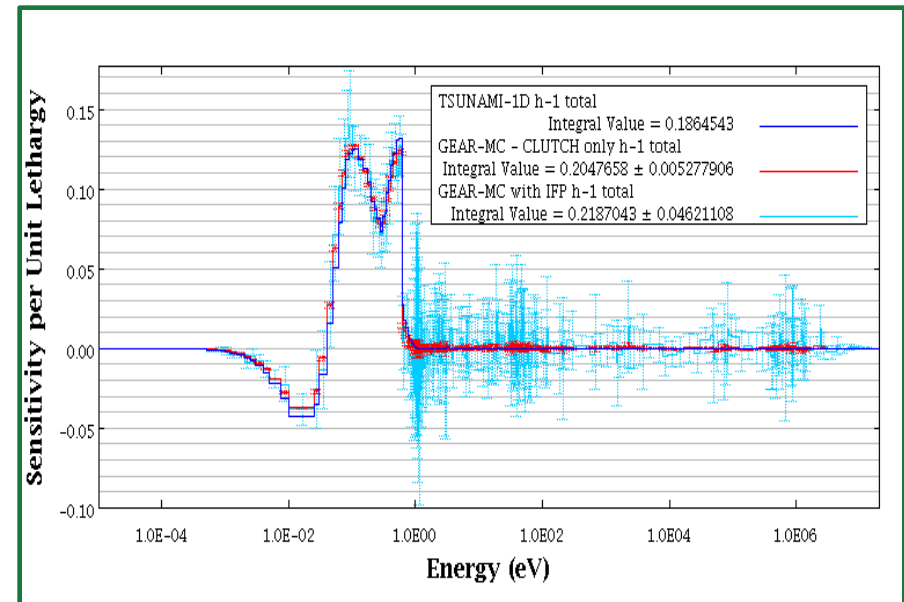
Model	GEAR-MC with IFP	GEAR-MC CLUTCH only	Memory Reduction
Godiva	581 MB	2.8 MB	99.52%
Flattop	1,082 MB	5.2 MB	99.52%
Fuel Pin	6,358 MB	3.2 MB	99.95%

Computational Efficiency

- Moving to a CLUTCH-only approach resulting in significantly improved computational efficiency for several cases.
- The Flattop calculations experienced an unexpected drop in efficiency when using an $F^*(r)$ mesh.

GEAR-MC Performance Metrics

Model	Average Runtime (hours)		Average Speedup
	IFP	CLUTCH	
Godiva	328.2	165.3	26.0
Flattop	261.1	197.1	0.52
Fuel Pin	191.4	44.1	10.25

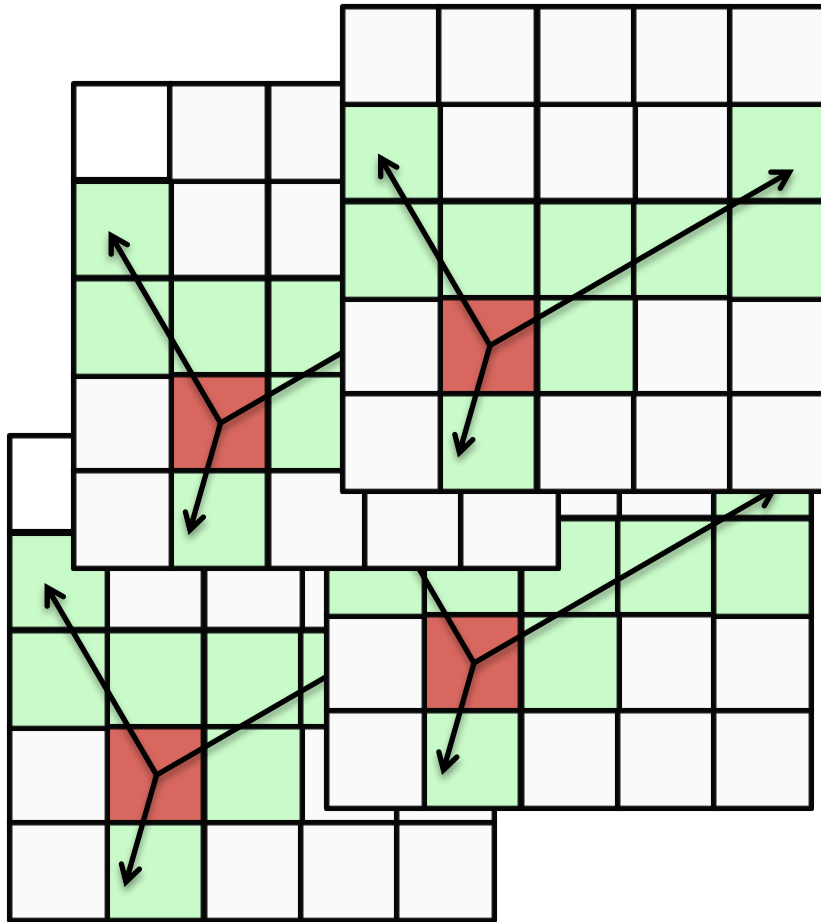


Fuel Pin Thermal Fission Cross-Section Sensitivity to H-1

Scaling and Memory Usage

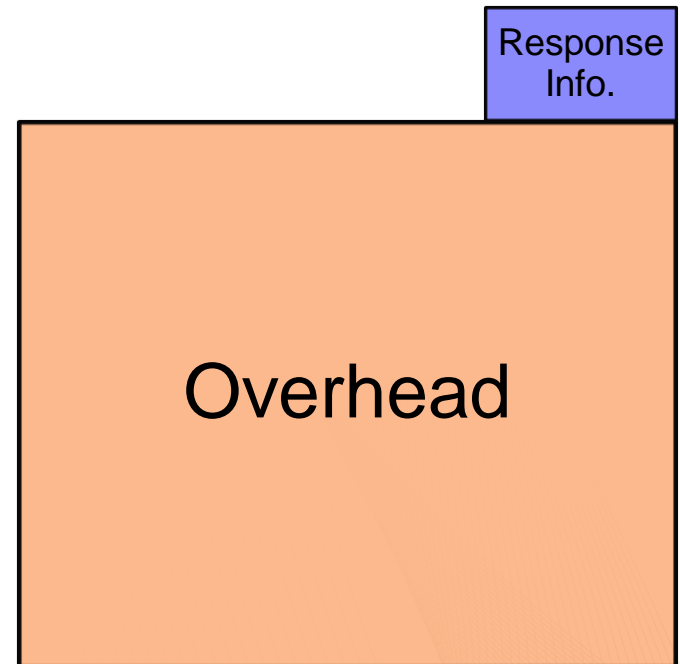
CLUTCH

One $F^*(r)$ Mesh per Response



IFP

Large Initial Overhead,
Low Additional Memory
per Response



Conclusions and Future Work

- The recently developed GEAR-MC method presents a first-of-its-kind approach for calculating sensitivity coefficients for generalized neutronic responses using continuous-energy, 3D Monte Carlo methods.
- The $F^*(r)$ mesh approach, which was originally developed for CLUTCH eigenvalue sensitivity calculations, was successfully extended to GEAR-MC GPT calculations.
- Removing the need to perform IFP calculations significantly reduced the memory footprint and, in some instances, improved the efficiency of the sensitivity calculations.
- The best approach for GEAR-MC calculations is likely problem-dependent, and $F^*(r)$ meshes in systems that are physically large, require a finely-resolved mesh, or contain a large number of responses may create significant memory footprints.

Questions???

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